# **Thermodynamic and crystallographic discussion of the formation and dissociation of zircon**

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The mechanism for the formation of zircon from a system of  $Si(OC_2H_5)_4-ZroCl_2 \cdot 8H_2O C_2H_5OH$  solution was constituted from the following steps; the formation of sol composed of an equimolar  $Zr^{4+}$  located in the neighbourhood of a linear siloxane polymer, deposition of metastable fine (tetragonal) T-ZrO<sub>2</sub> by heating, the tetragonal to monoclinic (T  $\rightarrow$  M) transformation of the fine  $T$ -ZrO<sub>2</sub> aggregates separated from the strain energy of grain boundary between two oxide components, the initiation of the interface reaction between  $T-ZrO<sub>2</sub>$  and amorphous  $SiO<sub>2</sub>$ , and the acceleration of the formation by the Hedvall effect caused by the crystallization of SiO<sub>2</sub>. The key technology for the synthesis of zircon from the oxide components ZrO<sub>2</sub> and SiO<sub>2</sub> was the mechanochemical activation of the surface layer by milling, the formation of transition phase between the two components by adding the guest element, and the presentation of metamorphic surface state. Zircon dissociated into M-ZrO<sub>2</sub> and SiO<sub>2</sub> glass, and the dissociation temperature was expected to be above 1700°C, which required the correction of the phase diagram for  $ZrO_2-SiO_2$  system used previously.

# **1. Introduction**

The zircon ceramic is an important candidate for high temperature refractory materials, because of its high thermal shock resistance, originating from having a lower thermal expansion coefficient than any other oxide ceramic. But, the thermal dissociation of zircon at higher temperatures is also known. In the presence of impurities, the dissociation temperature is remarkably lowered and the degree of it is elevated [1, 2]. It is said that the impurities showing a high reactivity towards silica have a strong effect on the dissociation phenomena [3].

Butterman and Foster [4] reported that the dissociation temperature was 1676  $\pm$  7°C. Further, in their study of the dissociation and the re-binding of zircon from Florida, Curtis and Sowman [5] reported that the dissociation started at  $1540^{\circ}$ C and almost all of it had dissociated by  $1870^{\circ}$  C, with a rapid increase in the rate from 1750°C.

The dissociation phenomena transforming it into monoclinic (M-)  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  glass was considerably influenced by the heating time. For example, the dissociation was almost finished by prolonged heating for 6 h at  $1760^{\circ}$  C. On the other hand, the degree of dissociation is also concerned with an undercooling rate, because of the re-binding of dissociated compounds, which is possible only under a very slow undercooling.

The powders purified from natural zircon sand have been used to investigate the thermal stability and the thermodynamic character of zircon. The natural zircon sand contains various impurities, such as  $HfO<sub>2</sub>$ , TiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, Fe<sub>2</sub>O<sub>3</sub>, CaO, MgO, P<sub>2</sub>O<sub>5</sub> [6], but of course, the purified powders are not perfectly free from the impurities. Therefore, it is expected that the dissociation temperature of synthesized zircon is higher than the previously published values [4, 5]. This rise would contribute to the expansion of the application fields of zircon ceramics.

In the synthesis of zircon by the sol-gel method from a  $ZrOCl_2 \tcdot 8H_2O-Si(OC_2H_5)_4-C_2H_5OH$  solution system, we previously reported that metastable fine  $T-ZrO<sub>2</sub>$  and amorphous  $SiO<sub>2</sub>$  powders were obtained by heating and the  $T-ZrO<sub>2</sub>$  aggregates gradually transformed into  $M-ZrO<sub>2</sub>$  with a decrease in surface energy caused by the temperature increase [10, 11].

Generally, the formation of zircon from  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  was studied in view of the additive effect of the impurities being a low melting point such as alkali halide and transition metal oxides. Naturally, the addition of the impurities directly relates to the lowering of the dissociation temperature. In this work, zircon powders were synthesized from  $ZrO$ , and  $SiO<sub>2</sub>$ without reaction promoters, and the thermodynamic and the crystallographic explanation for the formation and the dissociation of zircon were stated.

## **2. Experimental procedure**

### 2.1. Synthesis of zircon by the sol-gel method

An equimolar solution of  $ZroCl<sub>2</sub> · 8H<sub>2</sub>O$  dissolved in hot ethanol and  $Si(OC<sub>2</sub>H<sub>5</sub>)<sub>4</sub>$  was mixed using a magneate stirrer at room temperature. The rotation of stirrer was hindered by the increase in viscosity with an agitation time. Then the gel was allowed to dry in air, and then the dried gel was milled using a teflon ball and pot for 2 days. The milled powders were calcined in an ultra-high temperature electric furnace (Siliconit Co. Ltd Kogyo, Japan) at a heating rate of  $300^{\circ}$  C h<sup>-1</sup> under a carrier gas flow of clean air. It was



*Figure 1* XRD patterns of non-milling  $ZrO<sub>2</sub>-SiO<sub>2</sub>$  system powders calcined at (a) 1500, (b) 1650, (c) 1700°C.  $Zr = ZrSiO<sub>4</sub>$ ; M- $M-ZrO<sub>2</sub>; T- = T-ZrO<sub>2</sub>; Crist. = crystalite.$ 

kept for 2h at the desired temperature, and then cooled in the furnace under an air flow. The resultant powders were characterized by X-ray diffraction XRD (Rigaku Denki Co. Ltd.) using  $CuK\alpha$  radiation.

#### **2.2. Thermal dissociation of zircon**

The dissociation was investigated using the commercial zircon powders (Wako Junyaku Co. Ltd) of purity > 90%, manufactured through size reduction, purification and a calcination process of the natural zircon sand. The zircon powders were heated for 2 h at the desired temperatures under an air flow. The resultant powders were similarly characterized by XRD.

# **3. Results and discussion**

## 3.1. **Formation reaction of zircon**

Figure 1 shows the representative XRD patterns of non-milling powders synthesized by calcining at 1500, 1650 and 1700°C. The zircon crystal was barely formed at  $1500^{\circ}$ C, the conspicuous growth of the crystal was unrecognized till 1650°C, and then the zircon formation rapidly advanced by the interface reaction between T-ZrO<sub>2</sub> and crystobalite at  $1700^{\circ}$ C. It was recognized that the zircon formation by the interface reaction is difficult in the absence of a reaction promoter. This difficulty is easily explained by the crystallographic consideration, as illustrated in Fig. 2, showing a crystal structure of (a)  $T-ZrO<sub>2</sub>$  and (b)  $ZrSiO<sub>4</sub>$ .

In a case of  $T-ZrO<sub>2</sub>$ , the cations are displaced in the face-centred cubic form, and are located in the centre of the cube formed by the anions. The anions exist in the centre of regular tetrahedral formed by cations. The 8-coordination of zirconium is strained in the direction of the little arrows.

If both the movement of  $Zr^{4+}$  in the direction of the arrows, and the formation of the island-like lattice of regular tetrahedral  $SiO<sub>4</sub>$  by the insertion of the  $SiO<sub>2</sub>$ component were permitted, the combination reaction between  $ZrO_2$  and  $SiO_2$ , i.e., the zircon formation, was propagated. This crystallographic consideration supports the fact that an activation energy for the combination reaction between  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  is kinetically very large, so the combination reaction is permitted only at higher temperatures.

The low reactivity of the interface reaction between  $ZrO<sub>2</sub>$  and SiO<sub>2</sub> is also explained by the solubility relationship of the oxides of aluminium and silicon being side by side in the periodic table. The solid solution of SiO<sub>2</sub> in ZrO<sub>2</sub> does not exceed  $0.1\%$  SiO<sub>2</sub> according to Lang *et al.* [7]. On the other hand, Alper *et al.* [8] indicated that  $\langle 1\% \rangle$  ZrO<sub>2</sub> went into solid solution in  $\alpha$ -Al<sub>2</sub>O<sub>3</sub>, and up to  $\approx$  7% Al<sub>2</sub>O<sub>3</sub> could form solid solution with  $ZrO<sub>2</sub>$ . This solubility limit of the two compound systems let us estimate that the interface reaction of the  $ZrO<sub>2</sub>-SiO<sub>2</sub>$  system is inferior to that of the  $ZrO_2-Al_2O_3$  system in a reactivity. SiO<sub>2</sub> would be inferior to  $Al_2O_3$  with regard to the activation of a surface layer of  $ZrO<sub>2</sub>$ . In passing, the eutectic points of  $ZrO<sub>2</sub>-SiO<sub>2</sub>$  and  $ZrO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub>$  component systems are 1680, 1820°C, respectively [9] which contradict the reactivity between the solids.

Figure 3 shows (A) representative XRD patterns of milled powders synthesized by calcining at 1583 and 1700°C, and (B) the variation of  $I_p/(I_{ZR(200)} +$  $I_{M(11\bar{1})} + I_{M(11\bar{1})} + I_{T(11\bar{1})}$  [where  $P = ZR(200),$  $M(11\bar{1}) + M(111)$  or  $T(111)$ ] of the powders plotted against calcining temperature.

Here, I is the peak intensity of XRD, ZR is  $ZrSiO<sub>4</sub>$ , M- is  $M-ZrO<sub>2</sub>$ , T- is T-ZrO<sub>2</sub> and (abc) is the index of the crystal plane.

These patterns indicate that unreactive  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  remain in the absence of any promoters such as an alkali halide and transition metal, but it also suggests that the zircon formation is remarkably accelerated by the milling of dried powders. This milling effect is probably caused by the mechanochemical activation of the surface layer of dried powders and by the elevated mixing effect. However, we can not get a  $100\%$  ZrSiO<sub>4</sub> composite powder, because of the topochemical reaction often observed in the reaction between solids. It was estimated from Fig. 3 that the zircon formation is saturated in the temperature region above about  $1580^{\circ}$  C. Further investigation



*Figure 2* Crystallographic representation of the combination reaction between  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$ , (a) T-ZrO<sub>2</sub>, (b) ZrSiO<sub>4</sub> (fluorite structure). The little arrows  $(\uparrow)$  in the T-structure indicate the displacement of the oxygens from their positions in the c phase. Zirconiums are moved in the direction of  $(\uparrow)$ , and then islandlike lattice of  $SiO<sub>4</sub>$  are formed by the insertion of the  $SiO<sub>2</sub>$  component.



*Figure 3 (A)* XRD patterns of milled  $ZrO<sub>2</sub> - SiO<sub>2</sub>$  system powders calcined at (a) 1583, (b) 1700°C. (B) Variation of  $I_p/[I_{ZR(200)} +$  $I_{M(1\,1)} + I_{M(1\,1)} + I_{T(1\,1)}$  of the milled powders with calcining temperature,  $p = \text{ZR}(200)$ ,  $M(11\bar{1}) + M(111)$  or  $T(111)$ ;  $Am = amorphous.$ 

would be needed on the second grinding after the preliminary calcination and the reform of the milling technique in order to get 100% zircon crystal powders without additives.

Fig. 3 also shows the following important item, that is, the zircon formation by the combination between crystobalite and T-ZrO<sub>2</sub> is possible even at  $1700^{\circ}$ C without the thermal dissociation. Besides, Fig. 1 shows that the change of Gibb's free energy for the formation reaction of zircon at  $1700^{\circ}$ C is a negative value. This would suggest that the dissociation temperature of zircon is above  $1700^{\circ}$ C.

In the previous papers [10, 11], we investigated the formation mechanism of  $ZrSiO<sub>4</sub>$  synthesized from a  $Si(OC_2H_5)_4$ -ZrOCl<sub>2</sub> ·  $8H_2O-C_2H_5OH$  system solution in relation to the  $T \rightarrow M$  transformation of

<sup>1580</sup>  $ZrO_2$  and to the crystallization of SiO<sub>2</sub>, where the<br><sup>2</sup><br> $\begin{array}{c|c} \text{Crist.} \\ \hline \text{A-ZrO}_2 \\ \hline \text{A-ZrO}_2 \\ \end{array}$  Fig. 3B, consisted of four steps; that is, amorphous formation scheme of zircon (zone 1-3), described in Fig. 3B, consisted of four steps; that is, amorphous  $SiO<sub>2</sub> + T-ZrO<sub>2</sub>$ , crystobalite + T-ZrO<sub>2</sub> (Hedvall effect caused by crystallization of  $SiO<sub>2</sub>$ ), crystobalite + T-ZrO<sub>2</sub>, crystobalite + M-ZrO<sub>2</sub>\* (\* estimation) with a temperature increase.

> Kadogawa and Yamate [12] synthesized zircon powders (100%) free from residual  $ZrO_2$  and SiO, by the sol-gel method from a system of  $Si(OC<sub>2</sub>H<sub>5</sub>)<sub>4</sub>$ - $ZrOCl_2 \cdot 8H_2O-H_2O-Ni(NO_3)$ ,  $6H_2O-HCl$  (catalyst) in a low temperature region. The zircon formation proceeded from amorphous  $SiO<sub>2</sub> + T-ZrO<sub>2</sub>$ , then  $M-ZrO<sub>2</sub>$  contributed to the formation according to the shortage of  $T-ZrO<sub>2</sub>$  consumed, and resulted in zircon powders (100%). This successful synthesis of zircon free from residual oxides is probably due to the effect of transition metal ion standing at the grain boundary between  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$ , for the metallic impurities tend to concentrate to the boundary.

> Let us discuss again zone  $3$  (crystobalite +  $T-ZrO<sub>2</sub>$ ) in Fig. 3. If we want to obtain the zircon powders (100%), the interface reaction between  $M-ZrO<sub>2</sub>$  and crystobalite is needed according to the lack of T-ZrO<sub>2</sub> consumed by the zircon formation. This mechanism would be possible by suitable choice of grinding condition of dried powders and/or by twice grinding after preliminary calcination. This speculation is based on the idea that the interface reaction between  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  depends on the surface state of two component oxides.

> The recombination of dissociated  $ZrO<sub>2</sub>$  and SiO<sub>2</sub> has been investigated by many researchers [13, 14], who reported that the recombination is rapidly accelerated from  $1450^{\circ}$  C. Easy recombination of dissociated  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  indicates that the zircon synthesis is readily performed, if the surface state of two component oxides is metamorphic. It is said that the surface structure of the dissociated  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  is slightly destroyed, i.e., presents a metamorphic state. Therefore, it is estimated that the synthesis reaction of zircon is strongly affected by the disturbed lattice structure, simultaneously considering the milling effect for the reaction promotion. The dissociation of zircon is remarkably promoted by the penetration of additive oxide components to the interface layer (at a lower temperature) and to the bulk of zircon crystal (at a higher temperature), which means that the formation and the dissociation of zircon is a very sensitive reaction for the surface state.

Next, we will consider the difference in reactivity of



*Figure 4* Crystal structure of  $ZrO$ <sub>2</sub> polytype (a) M-(7-coordination); (b) T-(8-coordination).



*Figure 5* XRD patterns of commercial zircon powders heated at (a) 1500, (b) 1650, (c) 1700°C.

the  $ZrO<sub>2</sub>$  polytype against  $SiO<sub>2</sub>$  from the crystallographic aspect. Fig. 4 shows the crystal structure of  $ZrO<sub>2</sub>$ , (a) M-(7-coordination), (b) T-(8-coordination). The 7-coordination of  $M-ZrO<sub>2</sub>$  has a directional bonding character. The crystal structure of  $T-ZrO<sub>2</sub>$  is strained in the direction of the arrow in Fig. 4b. The coordination number of zirconium in the zircon crystal is 8, therefore it is suspected that  $T-ZrO<sub>2</sub>$  having 8-coordination is more favourable for the zircon formation reaction in view of the migration of atoms.

Another geometrical factor, but crystallographic aspect, should be considered on the favourability of  $T-ZrO<sub>2</sub>$  for the synthesis reaction of zircon. We formerly reported that the heat-treated powders were a mixture of metastable fine  $T-ZrO<sub>2</sub>$  and amorphous  $SiO<sub>2</sub>$ . The T-ZrO<sub>2</sub> aggregates were then gradually transformed into  $M-ZrO<sub>2</sub>$  with an increase in temperature because of the decrease in excess surface energy; the metastable  $T-ZrO$ , existed in the neighbourhood of  $SiO<sub>2</sub>$  as it was stabilized with the aid of the strain energy of grain boundary between  $SiO<sub>2</sub>$  and  $ZrO<sub>2</sub>$ . The fine  $T-ZrO<sub>2</sub>$  particles separated from the strain energy tend to aggrolimate, following the  $T \rightarrow M$ transformation [11, 15]. After all,  $T-ZrO<sub>2</sub>$  located in the neighbourhood of  $SiO<sub>2</sub>$  particles contributes to the formation reaction of zircon at a lower temperature, and  $M-ZrO<sub>2</sub>$  perhaps contributes to the reaction at a higher temperature. This is another geometrical reason for the favourability of  $T-ZrO<sub>2</sub>$  against the zircon synthesis.

### **3.2. Dissociation of commercial zircon**  powder

Fig. 5 shows the XRD patterns of commercial zircon powders heated at 1500, 1650 and 1700°C. The dissociation of zircon did not occur below  $1650^{\circ}$ C, but the zircon dissociated into  $M-ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$  glass at  $1700$ <sup>o</sup> C. The starting temperature of the dissociation (1650-1700°C) is largely different from the value (1540°C) of Curtis and Sowman [5], but roughly agreed with that (1676  $\pm$  7°C) of Butterman and Foster [4]. This difference may be due to the metallic impurities. The dissociation temperature of zircon powders purified from the natural sand would be further elevated by better techniques for removing the impurities. As the synthesized zircon powders did not dissociate in spite of the 1700°C treatment, there is a

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TABLE I The change in standard Gibb's free energy for the formation of zircon from  $ZrO_2$  and  $SiO_2$  by Rosén and Muan [16]

Temperature $(^{\circ}C)$	! 180	1242	1300	1366
$-\Delta G_T^0$ (Keal mol <sup>-1</sup> )	2.38	1.98	-64	1.29

 $(1 \text{ K cal mol}^{-1} = 4.187 \text{ KJ mol}^{-1})$ 

possibility that the high performance zircon ceramics suppressed the thermal dissociation.

## 3.3. Thermochemical analysis of dissociation temperature

In the investigation on stability of zircon in the temperature range 1180 to 1366°C, Rosén and Muan [16] developed an experimental method to determine the change in standard Gibb's free energy ( $-\Delta G_{\tau}^0$ ) for the formation of zircon from oxide components  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$ , where the method consisted in equilibrating metallic cobalt, a  $CO<sub>2</sub>/CO$  ratio of the gas phase, and chosen phase assembles in the system  $CoO-ZrO<sub>2</sub>$ -SiO<sub>2</sub> and CoO-SiO<sub>2</sub>. They gave  $-\Delta G_T^0$  as shown in Table I, and estimated that the dissociation temperature was 1600 to 1650°C from an extrapolation of the curve.

From the thermochemical analysis on the basis of calculation of  $\Delta S_T^0$ ,  $\Delta H_T^0$ ,  $\Delta G_T^0$  for the reaction (where  $\Delta S$  and  $\Delta H$  are the entropy and enthalpy, respectively), Matwejew *et al.* [17] estimated that the dissociation temperature was in the range of 1527-1927°C from the extrapolation method. Where  $\Delta S_T^0$  was calculated as follows (using heat capacity values,  $C_p$ ):

$$
\Delta S_T^0 = \Delta S_{298}^0 + \int_{298}^{348} \Delta C_p^{\prime} / T dT + \Delta S_I^0
$$
  
+ 
$$
\int_{848}^{1478} \Delta C_p^{\prime\prime} / T dT + \Delta S_H^0 + \int_{1478}^T \Delta C_p^{\prime\prime\prime} / T dT
$$
 (1)

 $\Delta S_1^0$  = heat of  $\beta \rightarrow \alpha$  quartz transformation divided by 848

 $\overline{a}$ 

 $\Delta S_{11}^0$  = heat of M-ZrO<sub>2</sub>  $\rightarrow$  T-ZrO<sub>2</sub> transformation divided by 1478

$$
\Delta C_p' = C_{p,ZrSiO_4} - C_{p,M-ZrO_2} - C_{p,\beta\text{-quartz}},
$$
\n
$$
\Delta C_p'' = C_{p,ZrSiO_4} - C_{p,M-ZrO_2} - C_{p,\alpha\text{-quartz}},
$$
\n
$$
C_p''' = C_{p,ZrSiO_4} - C_{p,T-ZrO_2} - C_{p,\alpha\text{-quartz}},
$$
\n
$$
\Delta S_{298}^0 = S_{298,ZrSiO_4}^0 - S_{298,M-ZrO_2}^0 - S_{298,\beta\text{-quartz}}^0
$$

However, the extrapolation done by two groups [16, 17] was too rough. We calculated the dissociation temperature by analysing progressively the  $-\Delta G_T^0$ values of these two research groups in the previous paper [18]. As a result, the dissociation temperature was respectively estimated to be  $1707^{\circ}$  C (in the case of Rosén and Muan) and 1841°C (Matwejew et al.). The former value is fundamentally based on experimental data, the latter is due to a typical calculation of the entropy according to Equation 1. Judging from Figs 1 and 3, the dissociation temperature  $1707^{\circ}$ C is worthy of commendation. The deviation of the latter value  $(1831°C)$  is perhaps due to the difference between Equation 1 and the real formation mechanism in Fig. 3.



*Figure 6* Schematic representation of the formation of zircon from a system of  $Si(OC_2H_5)_4$ -ZrOCl<sub>2</sub> •  $8H_2O-C_2H_5OH$  solution. S = silica;  $Z =$  zirconia; a = amorphous; T- = tetragonal; M = monoclinic; ZR = zircon.

Rosén and Muan  $[16]$  reported that the ZrO<sub>2</sub> in the phase assemblage,  $Co_2SiO_4 + ZrO_2 + 2CO =$  $2Co + ZrSiO<sub>4</sub> + 2CO<sub>2</sub>$ , was the T-form and the SiO<sub>2</sub> in the phase assemblage,  $Co_2SiO_4 + 2CO = 2Co +$  $SiO<sub>2</sub> + 2CO<sub>2</sub>$ , was crystobalite. So, the  $-\Delta G_T^0$  for the reaction, T-ZrO<sub>2</sub> + crystobalite = ZrSiO<sub>4</sub>, is calculated from the thermochemicai data of three kinds of crystals [19-21], a dissociation temperature of 1609°C was obtained [18]. This value is very low and contradicts the results of Figs 1 and 3. This discrepancy would also arise from a difference of the formation mechanism.

#### 3.4. Calculation of dissociation temperature from the proposed mechanism

Based on the formation mechanism of zircon shown in Fig. 3, the dissociation temperature was calculated as a trial. The heat capacity data [19-21] of the  $ZrO<sub>2</sub>$ - $SiO<sub>2</sub>$  phase system involved in the formation mechanism is summarized in Table II.

The change in heat capacity,  $\Delta C_p = \Delta a + \Delta bT +$  $\Delta c T^{-2}$ , for the formation reaction  $ZrO<sub>2</sub> + SiO<sub>2</sub> =$  $ZrSiO<sub>4</sub>$  was described as follows;

$$
\Delta C_{\text{p,zone1}} = 0.30 + 0.24 \times 10^{-3} T - 8.08 \times 10^{5} T^{-2}
$$
  

$$
(\sim 1588 \text{ K})
$$
  

$$
\Delta C_{\text{p,zone2}} = -0.72 + 1.88 \times 10^{-3} T - 8.08 \times 10^{5} T^{-2}
$$

$$
(1588 \sim 1853 \text{ K})
$$
\n(1588 \sim 1853 \text{ K})

 $\Delta C_{\text{p}, \text{zone3}} = 0.44 + 0.08 \times 10^{-3} T - 4.72 \times 10^{5} T^{-2}$  $(1853 K \sim)$ 

It should be noted that the application region of temperature for the equation  $C_p = f(T)$  is not always maintained in a derivation of these equations.

$$
\Delta G_T^0 = \Delta H_0 - \Delta a T \ln T - (1/2) \Delta b T^2
$$
  
 
$$
- (1/2) \Delta c T^{-1} + yT
$$
 (2)

TABLE II Heat capacities of the  $ZrO<sub>2</sub>-SiO<sub>2</sub>$  system substances

 $\Delta H_T^0 = \Delta H_0 + \Delta aT + (1/2)\Delta bT^2 - \Delta cT^{-1}$  (3)

By using  $\Delta G_{1515}^0 = -1980$ ,  $\Delta G_{1573}^0 = -1640 \text{ cal mol}^{-1}$ in Table I, Equations 1 and 2 are obtained.

$$
\Delta G_T^0 = -12170 - 0.30 T \ln T - 0.12 \times 10^{-3} T^2
$$
  
+ 4.04 × 10<sup>5</sup>T<sup>-1</sup> + 8.931T (~1588 K) (4)

$$
\Delta H_T^0 = -12170 + 0.3T + 0.12 \times 10^{-3} T^2
$$

$$
+ 8.08 \times 10^{3} T^{-1} \left( \sim 1588 \text{ K} \right) \tag{5}
$$

From Equations 4 and 5,  $\Delta G_{298}^{\circ} = -8674, \Delta H_{298}^{\circ} =$  $-$  9359 cal mol<sup>-1</sup> and thus  $\Delta S^{0}_{298} = 2.30$  cal mol<sup>-1</sup> K<sup>-1</sup> are obtained. Next,  $\Delta H_{1588}^{\circ} = -10882 \text{ cal mol}^{-1}$  is calculated from Equation 5. Therefore,

$$
\Delta H_T^0 = -12620 - 0.72 T + 0.94 \times 10^{-3} T^2
$$
  
+ 8.08 × 10<sup>5</sup> T<sup>-1</sup> (1588 ~ 1853 K) (6)

From Equation 6,  $\Delta H_{1853}^0 = -10290 \text{ cal mol}^{-1}$  is calculated, then

$$
\Delta H_T^0 = -11497 + 0.44 T + 0.04 \times 10^{-3} T^2
$$
  
+ 4.72 × 10<sup>5</sup>T<sup>-1</sup> (1853 K  $\sim$ ) (7)

On the other hand,  $\Delta S_T^0$  is determined as follows:

$$
\Delta S_T^0 = \Delta S_{298}^0 + \int_{298}^{1588} (\Delta C_{p, \text{zone1}}/T) dT + \Delta H_{tr}/1588
$$
  
+ 
$$
\int_{1588}^{1853} (\Delta C_{p, \text{zone2}}/T) dT
$$
  
+ 
$$
\int_{1853}^T (\Delta C_{p, \text{zone3}}/T) dT
$$
 (8)

Here  $\Delta H_{\text{tr}}$  is the crystallization heat for the transformation of amorphous  $SiO<sub>2</sub>$  to crystobalite, and it is assumed to be  $310 \text{ cal mol}^{-1}$  being the transformation heat of crystabolite. In Equation 8, the transformation heat of  $ZrO<sub>2</sub>$  is independent of the change in entropy for the formation of zircon, because  $M-ZrO<sub>2</sub>$  already exists as a starting crystal in zone 3, prior to the formation reaction. From Equations 7 and 8,  $\Delta H_{2100}^0$  =



 $M-$  = monoclinic;  $T-$  = tetragonal.

 $-10170$  cal mol<sup>-1</sup>,  $\Delta S^{0}_{2100} = -3.7855$  cal mol<sup>-1</sup> K<sup>-1</sup> are calculated, and so  $\Delta G_{2100}^{\circ} = -2220 \text{ cal mol}^{-1}$  is determined.

The calculated value of  $\Delta G_{2100}^0 = -2220$  was so low that we could barely obtain  $\Delta G_T^0 = 0$ , i.e. the dissociation temperature in a higher temperature region than 1831°C described formerly.

The thermochemical trial following the proposed mechanism resulted in failure. The major reason of the failure lay in ignoring the temperature range of application for the equation  $C_p = f(T)$ . This is the largest problem in the thermodynamics of fine particles. With decreasing the particle size, in general, the surface energy increases the binding energy of the crystal lattice, and the thermal vibration energy is superior to the kinematic one. The thermodynamic function of the fine system accompanying a negligible fluctuation caused by the variation of the surrounding environment should be corrected to some extent. Strictly speaking, the conventional thermodynamic function is valid only in the infinity of the system. Therefore, the determination of the dissociation temperature of the zircon synthesized from the sol-gel process, based on the classical thermodynamics, was unreasonable.

#### **4. Conclusion**

The mechanism for the formation of zircon from a system of  $Si(OC<sub>2</sub>H<sub>5</sub>)<sub>4</sub>-ZrOCl<sub>2</sub> · 8H<sub>2</sub>O-C<sub>2</sub>H<sub>5</sub>OH$  solution is schematically summarized in Fig. 6, considering the result described in the previous papers [21-24].

The state of the surface layer of the  $ZrO<sub>2</sub>$  and  $SiO<sub>2</sub>$ powders was very important in order to advance the combination reaction between two oxide components, and the following items were the most important for the reaction: (1) the mechanochemical activation of the surface layer by milling, (2) the formation of the transition phase between  $ZrO_2$  and  $SiO_2$  by the addition of a guest element, and (3) the presentation of a metamorhic state of the surface.

The calculation for the dissociation temperature should be performed for the zircon powders lacking residual ZrO<sub>2</sub> and SiO<sub>2</sub> and synthesized without additives, but the above calculation was a trial. The thermochemical analysis of the dissociation temperature followed by the proposed formation mechanism of zircon resulted in failure because of the fluctuation of the thermodynamic function generated in the fine system. The dissociation temperature of zircon was estimated to be above  $1700^{\circ}$ C, and the dissociated

zircon transformed into M-ZrO<sub>2</sub> and SiO<sub>2</sub> glass. These speculations led us to the correct form of the phase diagram for the  $ZrO<sub>2</sub>$ -SiO<sub>2</sub> system (Figs 362 and 2400) of [251).

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